

# PARSING

Baishakhi Ray

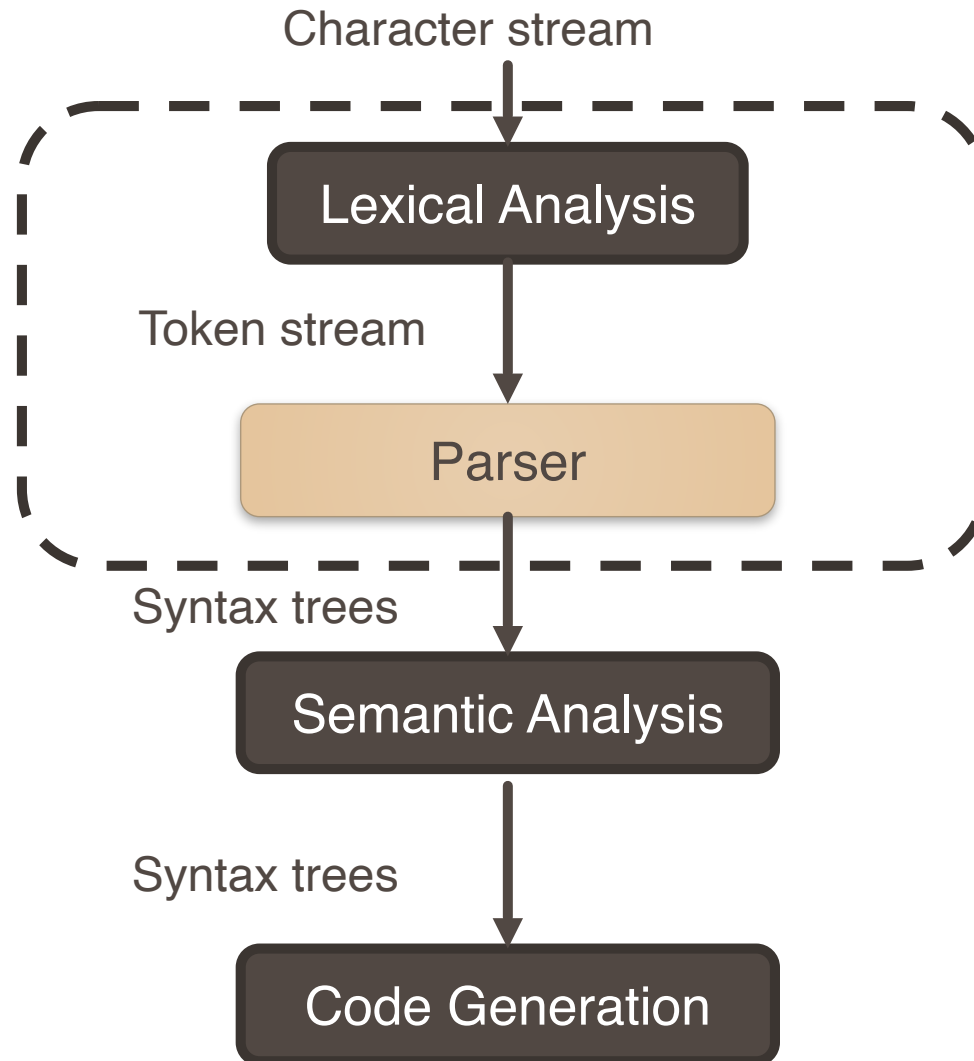
These slides are motivated from Prof. Alex Aiken: Compilers (Stanford)



- 
- $\langle \text{id}, x \rangle \langle \text{op}, * \rangle \langle \text{op}, \% \rangle$ 
    - Is it a valid token stream in C language?
    - Is it a valid statement in C language?

# Intro to Parsing

---



- Not every strings of tokens are valid
- Parser must distinguish between valid and invalid token strings.
- We need
  - A Language: to describe what is valid string?
  - A method: to determine membership of inputs in this language.

# Intro to Parsing

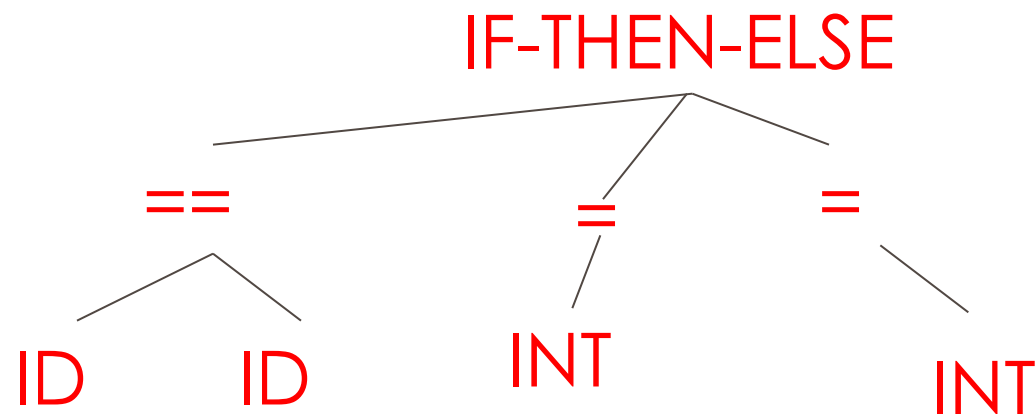
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- Input: if(x==y) 1 else 2;

- Parser Input (Lexical Input):

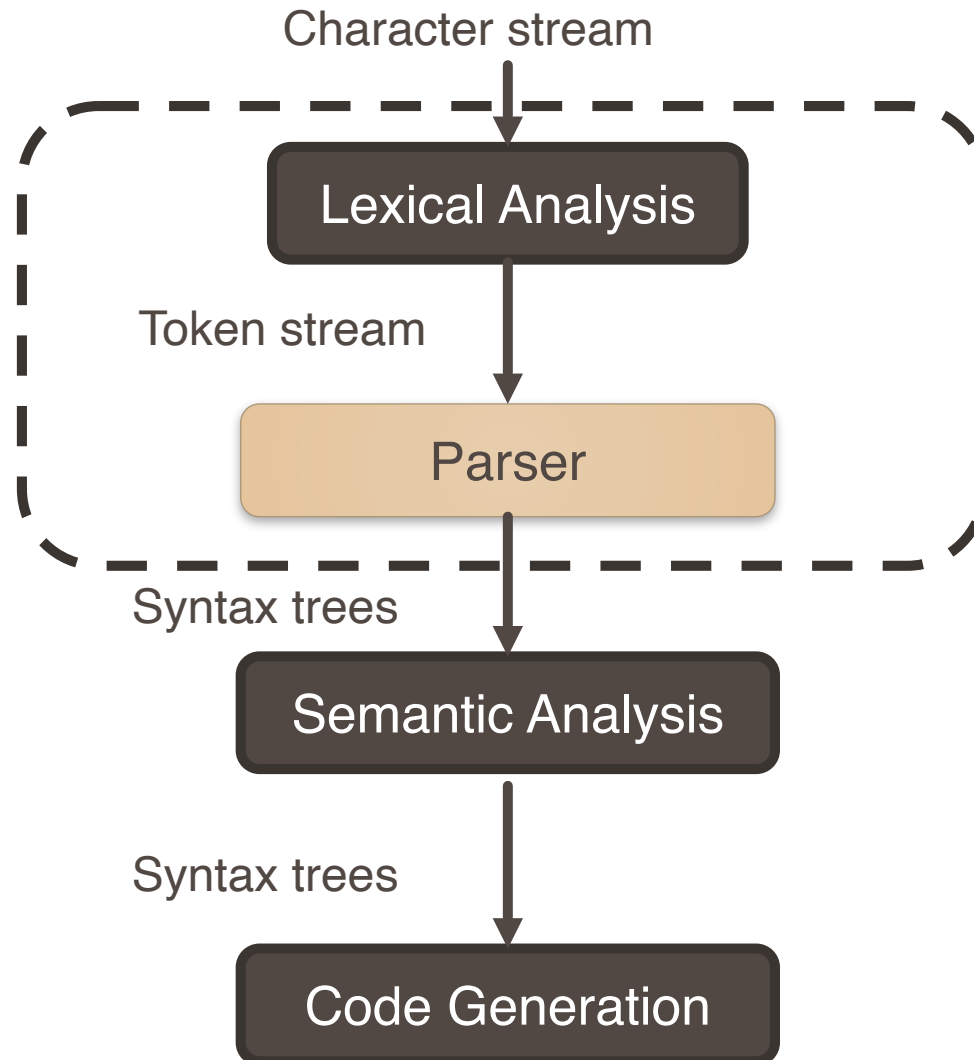
KEY(IF) '(' ID(x) OP('==') ')' INT(1) KEY(ELSE) INT(2) ';

- Parser Output



# Intro to Parsing

---



- Not every strings of tokens are valid
- Parser must distinguish between valid and invalid token strings.
- We need
  - A Language: to describe what is valid string?
    - Context Free Grammar
    - Capture Language Syntax
  - A method: to determine membership of inputs in this language.

# Context Free Grammar

---

- A CFG consists of
  - A set of terminal  $T$
  - A set of non-terminal  $N$
  - A start symbol  $S$  ( $S \in N$ )
  - A set of production rules
    - $X \rightarrow Y_1 \dots Y_N$
    - $X \in N$
    - $Y_i \in \{N, T, \varepsilon\}$
- Ex:  $S \rightarrow (S) \mid \varepsilon$ 
  - $N = \{S\}$
  - $T = \{ (, ) , \varepsilon \}$

# Context Free Grammar

---

1. Begin with a string with only the start symbol S
2. Replace a non-terminal X with in the string by the RHS of some production rule:

$$X \rightarrow Y_1 \dots Y_n$$

3. Repeat 2 again and again until there are no non-terminals

$$X_1 \dots X_i \underline{X} X_{i+1} \dots X_n \rightarrow X_1 \dots X_i Y_1 \dots Y_k X_{i+1} \dots X_n$$

For the production rule  $X \rightarrow Y_1 \dots Y_k$

$$\alpha_0 \rightarrow \alpha_1 \rightarrow \alpha_2 \rightarrow \alpha_3 \dots \rightarrow \alpha_n$$

$$\alpha_0 \xrightarrow{*} \alpha_n, n \geq 0$$

# Context Free Grammar

---

- Let  $G$  be a CFG with start symbol  $S$ . Then the language  $L(G)$  of  $G$  is:

$$\{a_1 \dots a_i \dots a_n \mid \forall i a_i \in T \wedge S \xrightarrow{*} a_1 \dots a_i \dots a_n\}$$



# Context Free Grammar

---

- There are **no rules** to replace terminals.
- Once generated, **terminals are permanent**
- Terminals ought to be tokens of programming languages
- Context-free grammars are a natural notation for this recursive structure

# Languages and Automata

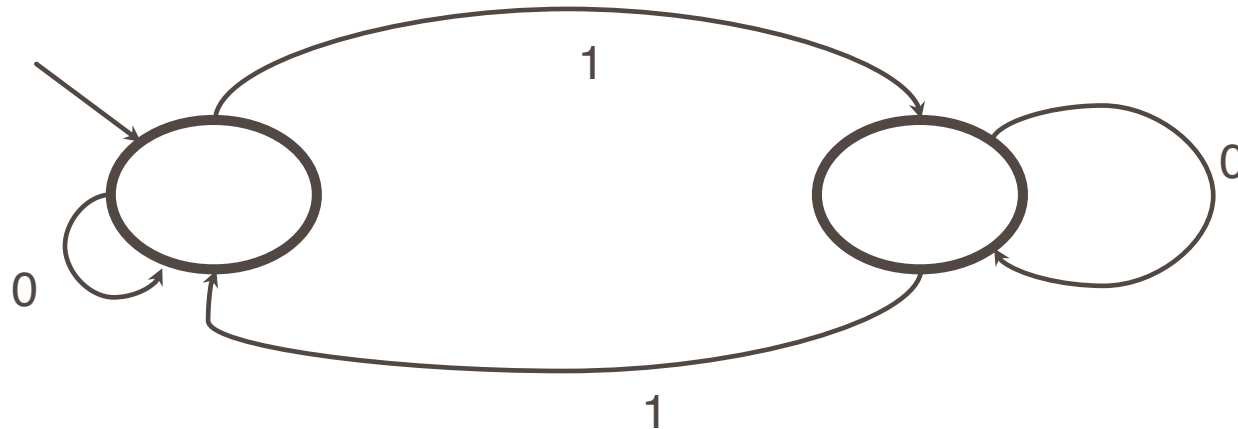
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- Formal languages are very important in programming languages
- Regular Languages
  - Weakest formal languages that are widely used
  - Many applications
- Many Languages are not regular

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Automata that accept odd numbers of 1



How many 1s it has accepted?

- Only solution is duplicate state

**Automata do not have any memory**

# Intro to Parsing

---

- Regular Languages
  - Weakest formal languages that are widely used
  - Many applications
- Consider the language  $\{(i)^i \mid i \geq 0\}$ 
  - $()$ ,  $(( ))$ ,  $(( ( )))$
  - $((1 + 2) * 3)$
- Nesting structures
  - if .. if.. else.. else..



Regular languages  
cannot handle well

## CFG: Simple Arithmetic expression

---

$E \rightarrow E + E$

|  $E * E$

|  $( E )$

| id

Languages can be generated: id, ( id ), ( id + id ) \* id, ...

## CFG: Exercise

---

$$S \rightarrow aXa$$

$$X \rightarrow \varepsilon \mid bY$$

$$Y \rightarrow \varepsilon \mid cXc$$

Some Valid Strings are: aba, abcca, ...

# Derivation

---

- A derivation is a sequence of production
  - $S \rightarrow \dots \rightarrow \dots \rightarrow$
- A derivation can be drawn as a tree
  - Start symbol is tree's root
  - For a production  $X \rightarrow Y_1 \dots Y_n$ , add children  $Y_1 \dots Y_n$  to node  $X$

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- Grammar

- $E \rightarrow E + E \mid E * E \mid (E) \mid id$

- String

- $id * id + id$

- Derivation

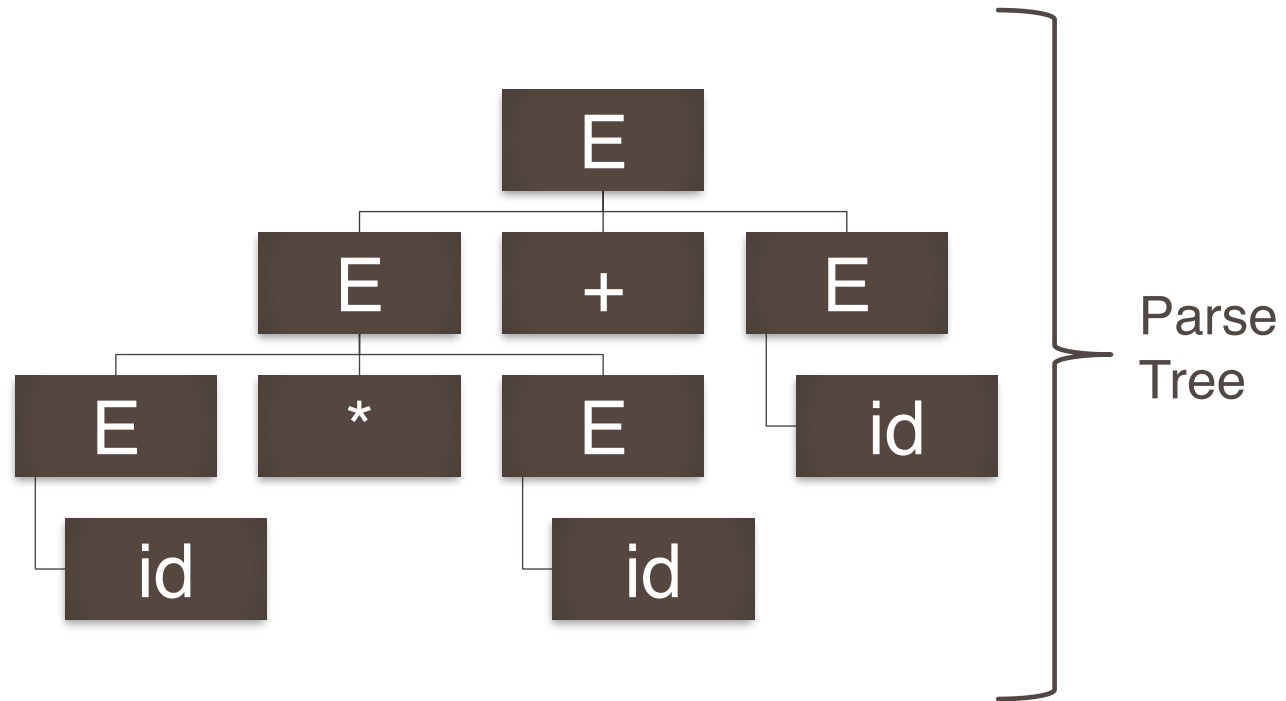
$E \rightarrow E + E$

$\rightarrow E * E + E$

$\rightarrow id * E + E$

$\rightarrow id * id + E$

$\rightarrow id * id + id$





# Parse Tree

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- A parse tree has
  - Terminals at the leaves
  - Non-terminals at the interior nodes
- An in-order traversal of the leaves is the original input
- The parse tree shows the association of operations, the input string does not

# Parse Tree

---

- Left-most derivation
  - At each step, replace the left-most non-terminal

$E \rightarrow E + E$

$\rightarrow E * E + E$

$\rightarrow id * E + E$

$\rightarrow id * id + E$

$\rightarrow id * id + id$

- Right-most derivation
  - At each step, replace the right-most non-terminal

$E \rightarrow E + E$

$\rightarrow E + id$

$\rightarrow E * E + id$

$\rightarrow E * id + id$

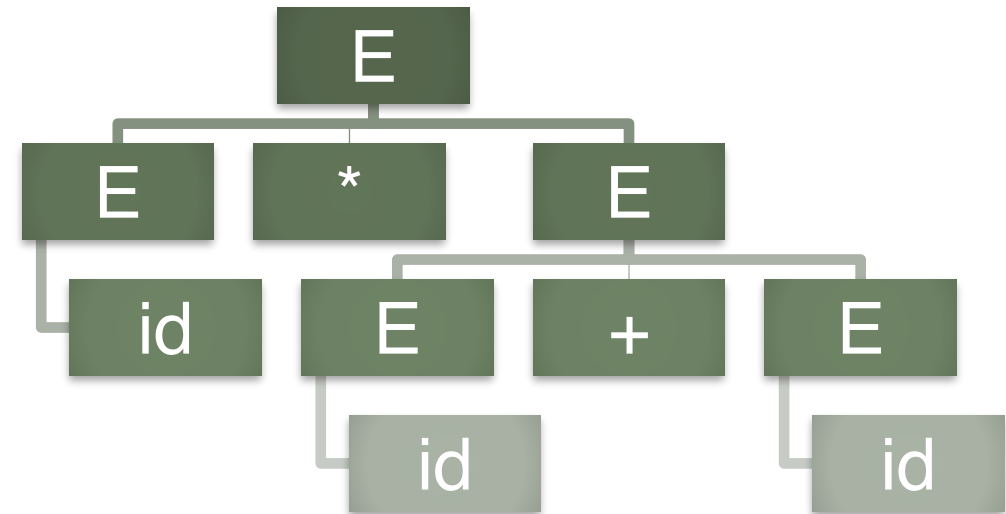
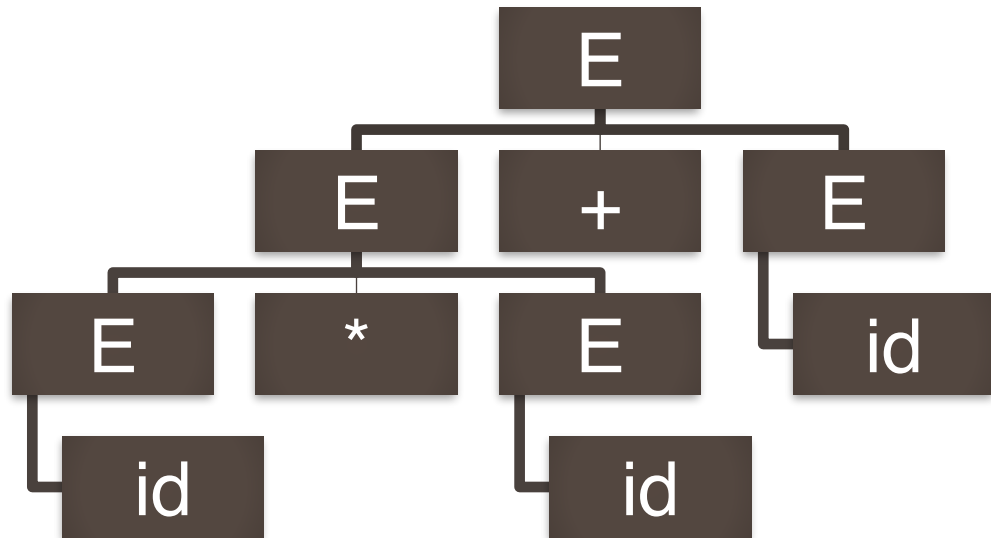
$\rightarrow id * id + id$

Note that, right-most and left-most derivations have the same parse tree

# Ambiguity

---

- Grammar
  - $E \rightarrow E + E \mid E * E \mid (E) \mid id$
- String
  - $id * id + id$



# Ambiguity

---

- A grammar is ambiguous if it has more than one parse tree for a string
  - There are more than one right-most or left-most derivation for some string
- Ambiguity is **bad**
  - Leaves meaning for some programs ill-defined

# Example of Ambiguous Grammar

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- $S \rightarrow SS \mid a \mid b$

# Resolving Ambiguity

---

- Most direct way to rewrite the grammar unambiguously

$id * id + id$

$$E = E' + E \mid E'$$

$$E' = id * E' \mid id \mid (E) * E' \mid (E)$$

# Resolving Ambiguity

---

- Impossible to convert ambiguous to unambiguous grammar automatically
- Instead of rewriting
  - Use ambiguous grammar
  - Along with disambiguating rules
    - Eg, precedence and associativity rules
    - Enforces precedence of \* over +
    - associativity: %left +

# Abstract Syntax Trees

---

- A parser traces the derivation of a sequence of tokens
- But the rest of the compiler needs a structural representation of the program
- Abstract Syntax Trees
  - Like parse trees but ignore some details
  - Abbreviated as AST



# Abstract Syntax Trees

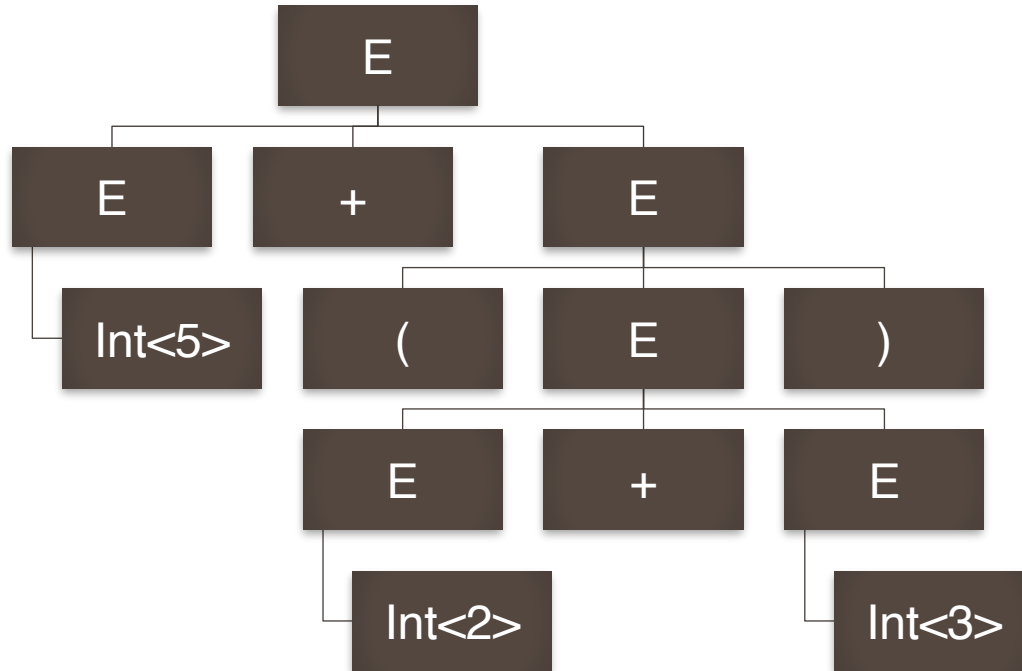
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- Grammar
  - $E \rightarrow \text{int} \mid ( E ) \mid E + E$
- String
  - $5 + (2 + 3)$
- After lexical analysis
  - $\text{Int}\langle 5 \rangle \text{'+' ' (' Int}\langle 2 \rangle \text{'+' Int}\langle 3 \rangle \text{' )'}$

# Abstract Syntax Trees: $5 + (2 + 3)$

---

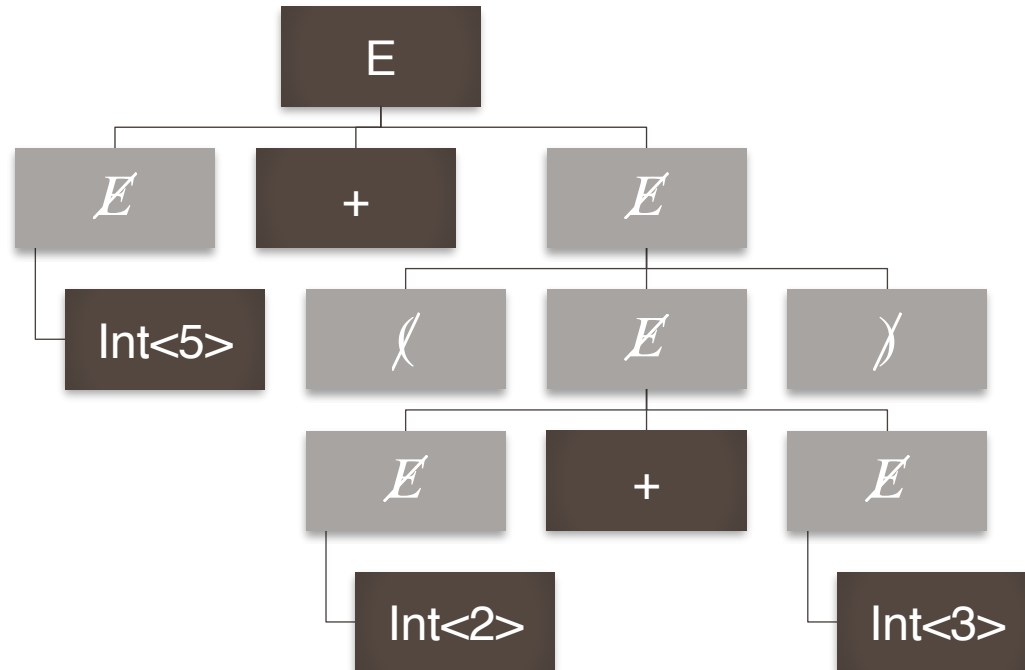
Parse Trees



# Abstract Syntax Trees: $5 + (2 + 3)$

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Parse Trees

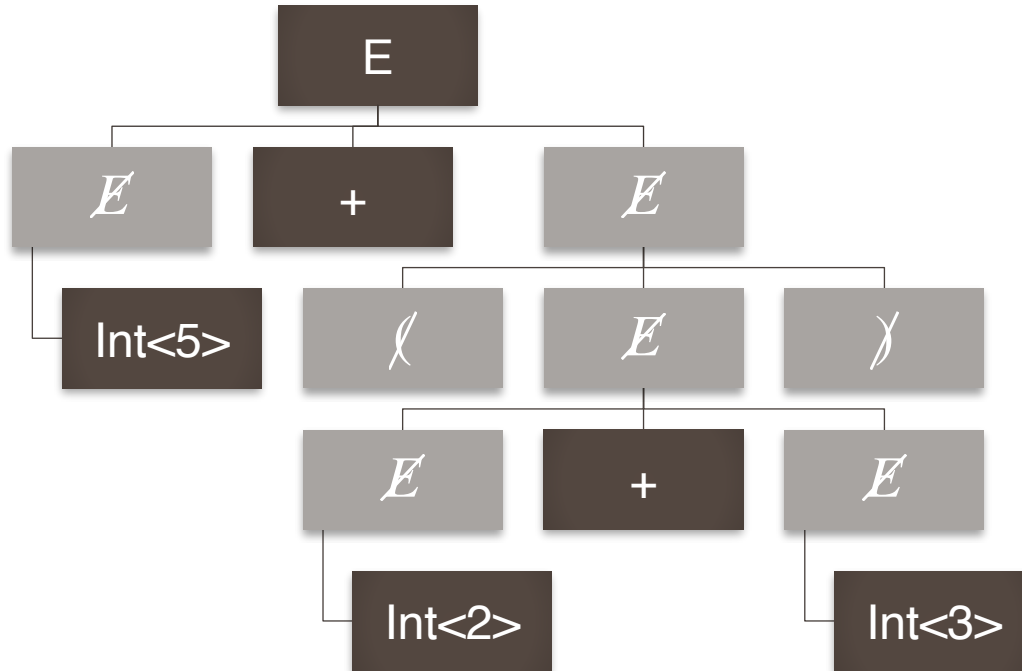


- Have too much information
  - Parentheses
  - Single-successor nodes

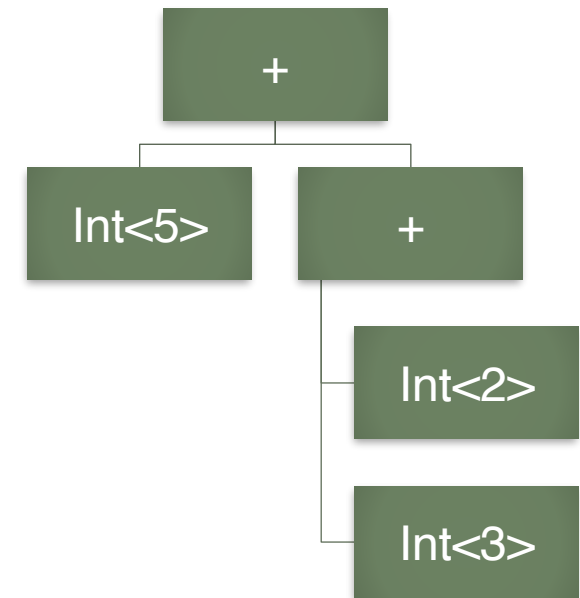
# Abstract Syntax Trees: $5 + (2 + 3)$

---

Parse Trees



AST



- Have too much information
  - Parentheses
  - Single-successor nodes

- ASTs capture the nesting structure
- But abstracts from the concrete syntax
  - More compact and easier to use

# Error Handling

---

- Purpose of the compiler is
  - To detect non-valid programs
  - To translate the valid ones
- Many kinds of possible errors (e.g., in C)

Error Kind		Example	Detected by
Lexical	Misspelling of identifiers, keywords, or operators.	... \$ ...	Lexer
Syntax	Misplaced operators, semicolons, braces, switch-case statements, etc.	... x*%...	Parser
Semantic	Type mismatches between operators and operands	... int x; y = x(3);...	Type Checker
Correctness	Incorrect reasoning	Using = instead of ==	tester/user

# Error Handling

---

- Error Handler should
  - Discover errors accurately and quickly
  - Recover from an error quickly
  - Not slow down compilation of valid code
  
- Types of Error Handling
  - Panic mode
  - Error productions
  - Automatic local or global correction

# Panic Mode Error Handling

---

- Panic mode is simplest and most popular method
- When an error is detected
  - Discard tokens until one with a clear role is found
    - Typically looks for “synchronizing” tokens
      - Typically the statement of expression terminators
      - Example: delimiters (; }, etc.)
  - Continue from there

# Panic Mode Error Handling

---

- Example:
  - $(1 + + 2) + 3$
- Panic-mode recovery:
  - Skip ahead to the next integer and then continue
- Bison: use the special terminal **error** to describe how much input to skip
  - $E \rightarrow \text{int} \mid E + E \mid ( E ) \mid \text{error int} \mid ( \text{error} )$





# Error Productions

---

- Specify known common mistakes in the grammar
- Example:
  - Write  $5x$  instead of  $5 * x$
  - Add production rule  $E \rightarrow .. \mid E E$
- Disadvantages
  - complicates the grammar

# Error Corrections

---

- Idea: find a correct “nearby” program
  - Try token insertions and deletions (goal: minimize edit distance)
  - Exhaustive search
- Disadvantages
  - Hard to implement
  - Slows down parsing of correct programs
  - “Nearby” is not necessarily “the intended” program

# Error Corrections

---

- Past

- Slow recompilation cycle (even once a day)
- Find as many errors in one cycle as possible

- Disadvantages

- Quick recompilation cycle
- Users tend to correct one error/cycle
- Complex error recovery is less compelling

# Parsing algorithm: Recursive Descent Parsing

---

- The parse tree is constructed
  - From the top
  - From left to right
  
- Terminals are seen in order of appearance in the token stream

# Parsing algorithm: Recursive Descent Parsing

---

- Grammar:
  - $E \rightarrow T \mid T + E$
  - $T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$
- Token Stream: ( int<5> )
- Start with top level non-terminal E
  - Try the rules for E in order

# Recursive Descent Parsing Example

---

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

E  
|  
T  
|  
int

mismatch: int does not match arrowhead (  
backtrack

( int<5> )

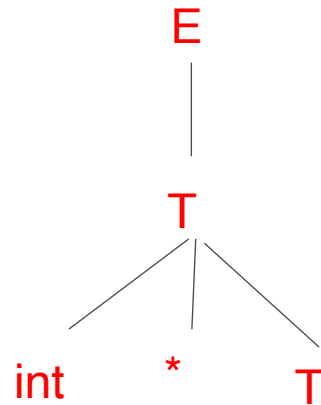


# Recursive Descent Parsing Example

---

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$



backtrack

( int<5> )

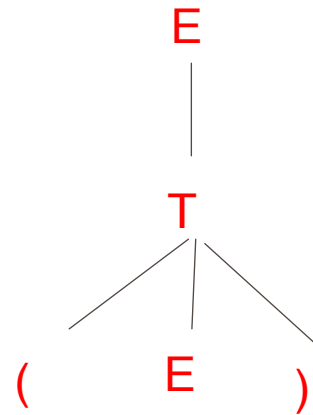


# Recursive Descent Parsing Example

---

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$



Match! Advance input

( int<5> )





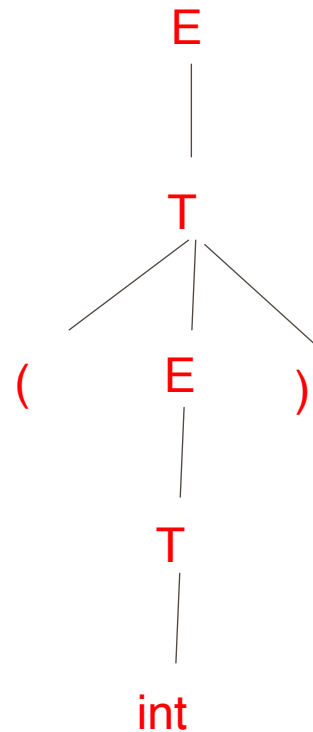
# Recursive Descent Parsing Example

---

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

( int<5> )



Match! Advance input

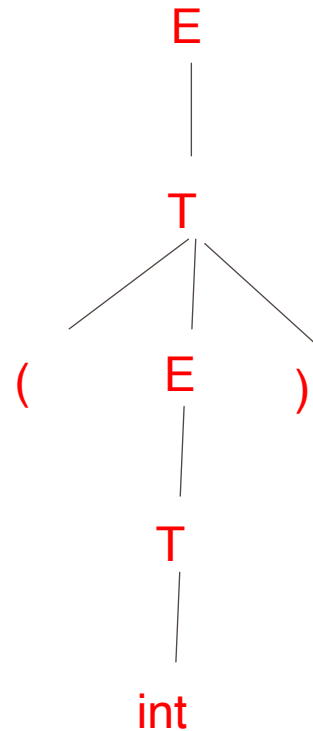
# Recursive Descent Parsing Example

---

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

( int<5> )  
↑



Match! Advance input

---

---

$$E \rightarrow E' \mid E' + E$$
$$E' \rightarrow -E' \mid id \mid (E)$$

Input: id + id

# A Recursive Descent Parser. Preliminaries

---

- **TOKEN:** type of tokens
  - Special tokens INT, OPEN, CLOSE, PLUS, TIMES
  
- The global next point to the next token

# A Top Down Parsing Algorithm

---

```
void A() {
```

```
    Choose an A-production:  $A \rightarrow S_1 S_2 \dots S_k$ ;
```

```
    for (i=1 or k) {
```

```
        if ( $S_i$  is a nonterminal)
```

```
            Call  $S_i()$ ;
```

```
        else if ( $X_i ==$  current input TOKEN tok). /*terminal*/
```

```
            next++;
```

```
    }
```

```
}
```

Recursion without  
backtracking

# A (Limited) Recursive Descent Parser

---

- Define boolean functions that check the token string for a match of

- A given token terminal

```
bool term (TOKEN tok) { return *next++ == tok; }
```

- The  $n^{\text{th}}$  production of S:

```
bool Sn() { ... }
```

- Try all productions of S:

```
bool S() { ... }
```

# A (Limited) Recursive Descent Parser

---

- For production  $E \rightarrow T$

```
bool E1() { return T(); }
```

- For production  $E \rightarrow T + E$

```
bool E2() { return T() && term(PLUS) && E(); }
```

- For all productions of E (with backtracking)

```
bool E() {  
    TOKEN *save = next;  
    return (next = save, E1( )) || (next = save, E2( ));  
}
```

Grammar:

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

# A (Limited) Recursive Descent Parser (4)

---

- Functions for non-terminal T

```
bool T1() { return term(INT); }
```

```
bool T2() { return term(INT) && term(TIMES) && T(); }
```

```
bool T3() { return term(OPEN) && E() && term(CLOSE); }
```

```
bool T() {
```

```
    TOKEN *save = next;
```

```
    return (next = save, T1()) || (next = save, T2()) || (next = save, T3());
```

```
}
```

Grammar:

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$



# Recursive Descent Parsing

---

- To start the parser
  - Initialize next to point to first token
  - Invoke  $E()$  (start symbol)

# Example

---

Grammar:

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

Input: ( int )

Code:

```
bool term(TOKEN tok) { return *next++ == tok; }
```

```
bool E1() { return T(); }
```

```
bool E2() { return T() && term(PLUS) && E(); }
```

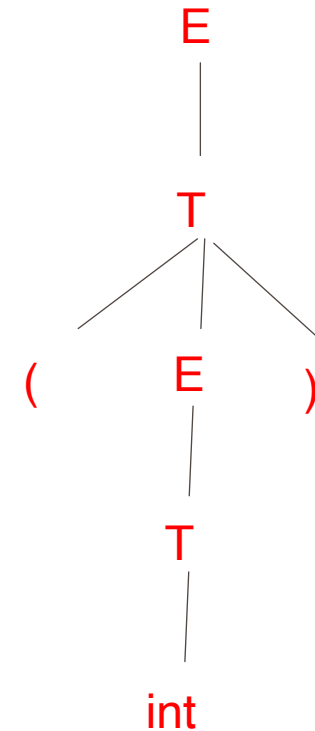
```
bool E() { TOKEN *save = next;  
         return (next = save, E1()) || (next = save, E2()); }
```

```
bool T1() { return term(INT); }
```

```
bool T2() { return term(INT) && term(TIMES) && T(); }
```

```
bool T3() { return term(OPEN) && E() && term(CLOSE); }
```

```
bool T() { TOKEN *save = next;  
         return (next = save, T1())  
             || (next = save, T2())  
             || (next = save, T3()); }
```



# Example

---

Grammar:

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

Input: `int`

Code:

```
bool term(TOKEN tok) { return *next++ == tok; }
```

```
bool E1() { return T(); }
```

```
bool E2() { return T() && term(PLUS) && E(); }
```

```
bool E() { TOKEN *save = next;  
         return (next = save, E1()) || (next = save, E2()); }
```

```
bool T1() { return term(INT); }
```

```
bool T2() { return term(INT) && term(TIMES) && T(); }
```

```
bool T3() { return term(OPEN) && E() && term(CLOSE); }
```

```
bool T() { TOKEN *save = next;  
         return (next = save, T1())  
             || (next = save, T2())  
             || (next = save, T3()); }
```

# When Recursive Descent Does Not Work

---

Grammar:

$E \rightarrow T \mid T + E$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

Input:  $\text{int} * \text{int}$

Code:

```
bool term(TOKEN tok) { return *next++ == tok; }

bool E1() { return T(); }
bool E2() { return T() && term(PLUS) && E(); }
bool E() {TOKEN *save = next;
         return (next = save, E1()) || (next = save, E2()); }

bool T1() { return term(INT); }
bool T2() { return term(INT) && term(TIMES) && T(); }
bool T3() { return term(OPEN) && E() && term(CLOSE); }
bool T() { TOKEN *save = next;
         return (next = save, T1())
            || (next = save, T2())
            || (next = save, T3()); }
```

# Recursive Descent Parsing: Limitation

---

- If production for non-terminal  $X$  **succeeds**
  - Cannot backtrack to try different production for  $X$  later
- General recursive descent algorithms support such full backtracking
  - Can implement any grammar
- Presented RDA is not general
  - But easy to implement
- Sufficient for grammars where for any non-terminal at most one production can succeed
- The grammar can be rewritten to work with the presented algorithm
  - By left factoring

# Left Factoring

---

$$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2$$

- The input begins with a nonempty string derived from  $\alpha$ , we do not know whether to expand  $A$  to  $\alpha\beta_1$  or  $\alpha\beta_2$ .
- We can defer the decision by expanding  $A$  to  $\alpha A'$ .
- Then, after seeing the input derived from  $\alpha$ , we expand  $A'$  to  $\beta_1$  or  $\beta_2$  (left-factored)
- The original productions become:

$$A \rightarrow \alpha A', A' \rightarrow \beta_1 \mid \beta_2$$

# Left Factoring

---

- Recall the grammar

$E \rightarrow T + E \mid T$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

- Hard to predict because
  - For T two productions start with int
  - For E it is not clear how to predict
- We need to left-factor the grammar

# Left-Factoring Example

---

- Grammar

$E \rightarrow T + E \mid T$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

- Factor out common prefixes of productions

$E \rightarrow T X$

$X \rightarrow + E \mid \varepsilon$

$T \rightarrow ( E ) \mid \text{int} Y$

$Y \rightarrow * T \mid \varepsilon$



# When Recursive Descent Does Not Work

---

- Consider a production  $S \rightarrow S a$   
`bool S1() { return S() && term(a); }`  
`bool S() { return S1(); }`
- S() goes into an infinite loop
- A **left-recursive grammar** has a non-terminal S  
 $S \rightarrow^+ Sa$  for some a
- Recursive descent does not work for left recursive grammar

# Elimination of Left Recursion

---

- Consider the left-recursive grammar

$$S \rightarrow S \alpha \mid \beta$$

- $S$  generates all strings starting with a  $\beta$  and followed by a number of  $\alpha$
- Can rewrite using right-recursion

$$S \rightarrow \beta S'$$

$$S' \rightarrow \alpha S' \mid \varepsilon$$

## More Elimination of Left-Recursion

---

- In general

$$S \rightarrow S \alpha_1 \mid \dots \mid S \alpha_n \mid \beta_1 \mid \dots \mid \beta_m$$

- All strings derived from  $S$  start with one of  $\beta_1, \dots, \beta_m$  and continue with several instances of  $\alpha_1, \dots, \alpha_n$

- Rewrite as

$$S \rightarrow \beta_1 S' \mid \dots \mid \beta_m S'$$

$$S' \rightarrow \alpha_1 S' \mid \dots \mid \alpha_n S' \mid \varepsilon$$

## General Left Recursion

---

- The grammar

$$S \rightarrow A \alpha \mid \delta$$

$$A \rightarrow S \beta$$

is also left-recursive because

$$S \rightarrow^+ S \beta \alpha$$

- This left-recursive can also be eliminated

# Example

---

- $S \rightarrow Aa \mid b$
- $A \rightarrow Ac \mid Sd \mid \epsilon$
- Remove Recursion.

- 
- $S \rightarrow Aa \mid b.$
  - $A \rightarrow bdA' \mid A'$
  - $A' \rightarrow cA' \mid adA' \mid a \mid \epsilon$

# Summary of Recursive Descent

---

- Simple and general parsing strategy
  - Left-recursion must be eliminated first
  - ... but that can be done automatically
- Unpopular because of backtracking
  - Thought to be too inefficient
- In practice, backtracking is eliminated by restricting the grammar

# Predictive Parsers

---

- Like recursive-descent but parser can “predict” which production to use
  - By looking at the next few tokens
  - **No backtracking**
- Predictive parsers accept LL(k) grammars
  - L means “left-to-right” scan of input
  - L means “leftmost derivation”
  - k means “predict based on k tokens of lookahead”
  - In practice, LL(1) is used



# LL(1) vs. Recursive Descent

---

- In recursive-descent
  - At each step, many choices of production to use
  - Backtracking used to undo bad choices
- In LL(1)
  - At each step, only one choice of production
  - That is
    - When a non-terminal  $A$  is leftmost in a derivation
    - The next input symbol is  $t$
    - There is a unique production  $A \rightarrow \alpha$  to use
      - Or no production to use (an error state)
- LL(1) is a recursive descent variant without backtracking

# Predictive Parsing and Left Factoring

---

- Recall the grammar

$E \rightarrow T + E \mid T$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

- Hard to predict because
  - For T two productions start with int
  - For E it is not clear how to predict
- We need to left-factor the grammar

# Left-Factoring Example

---

- Grammar

$E \rightarrow T + E \mid T$

$T \rightarrow \text{int} \mid \text{int} * T \mid ( E )$

- Factor out common prefixes of productions

$E \rightarrow T X$

$X \rightarrow + E \mid \varepsilon$

$T \rightarrow ( E ) \mid \text{int} Y$

$Y \rightarrow * T \mid \varepsilon$

# LL(1) Parsing Table Example

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- Left-factored grammar

$E \rightarrow T X$

$X \rightarrow + E \mid \varepsilon$

$T \rightarrow ( E ) \mid \text{int } Y$

$Y \rightarrow * T \mid \varepsilon$

- The LL(1) parsing table:

Left-most non- terminals		next input tokens						
		int	*	+	(	)	\$	
	E	TX				TX		
	X				+E		$\varepsilon$	$\varepsilon$
	T	int Y				( E )		
	Y			*T	$\varepsilon$		$\varepsilon$	$\varepsilon$

## LL(1) Parsing Table Example (Cont.)

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- Consider the [E, int] entry
  - “When current non-terminal is E and next input is int, use production  $E \rightarrow T X$ ”
  - This can generate an int in the first position
- Consider the [Y, +] entry
  - “When current non-terminal is Y and current token is +, get rid of Y”
  - Y can be followed by + only if  $Y \rightarrow \epsilon$

## LL(1) Parsing Tables. Errors

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- Blank entries indicate error situations
- Consider the  $[E, *]$  entry
  - “There is no way to derive a string starting with  $*$  from non-terminal  $E$ ”

# Using Parsing Tables

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- Method similar to recursive descent, **except**
  - For the leftmost non-terminal **S**
  - We look at the next input token **a**
  - And choose the production shown at **[S,a]**
- Reject on reaching error state
- Accept on end of input & empty stack

# Bottom-Up Parsing

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- Bottom-up parsing is more general than (deterministic) top-down parsing
  - just as efficient
  - Builds on ideas in top-down parsing
- Bottom-up parsers don't need left-factored grammars
- Revert to the “natural” grammar for our example:  
$$E \rightarrow T + E \mid T$$
$$T \rightarrow \text{int} * T \mid \text{int} \mid (E) \cdot$$
- Consider the string:  $\text{int} * \text{int} + \text{int}$



# Bottom-Up Parsing

---

- Revert to the “natural” grammar for our example:

$E \rightarrow T + E \mid T$

$T \rightarrow \text{int} * T \mid \text{int} \mid (E) \cdot$

- Consider the string:  $\text{int} * \text{int} + \text{int}$

- Bottom-up parsing **reduces** a string to the start symbol by **inverting** productions:

$\text{int} * \text{int} + \text{int}$

$T \rightarrow \text{int}$

$\text{int} * T + \text{int}$

$T \rightarrow \text{int} * T$

$T + \text{int}$

$T \rightarrow \text{int}$

$T + T$

$E \rightarrow T$

$T + E$

$E \rightarrow T + E$

$E$

# Observation

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- Read the productions in reverse (from bottom to top)
- This is a rightmost derivation!

int \* int + int

T → int

int \* T + int

T → int \* T

T + int

T → int

T + T

E → T

T + E

E → T + E

E

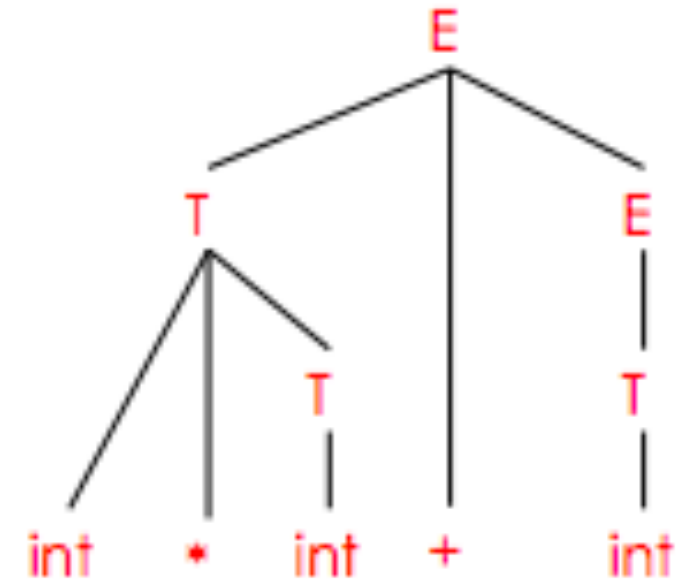
# Bottom-Up Parsing

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- A bottom-up parser traces a **rightmost derivation in reverse**

int \* int + int  
int \* T + int  
T + int  
T + T  
T + E  
E

T → int  
T → int \* T  
T → int  
E → T  
E → T + E



# L, R, and all that

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- LR parser: “Bottom-up parser”
- L = Left-to-right scan, R = Rightmost derivation
- RR parser: R = Right-to-left scan (from end)
  - nobody uses these
- LL parser: “Top-down parser”:
- L = Left-to-right scan: L = Leftmost derivation
- LR(1): LR parser that considers next token (lookahead of 1)
- LR(0): Only considers stack to decide shift/reduce
- SLR(1): Simple LR: lookahead from first/follow rules Derived from LR(0) automaton
- LALR(1): Lookahead LR(1): fancier lookahead analysis Uses same LR(0) automaton as SLR(1)